

There are bodies that carry "electricity"

two kinds $\begin{cases} \text{neg charged} \\ \text{pos charged.} \end{cases}$

The basic unit of charge

$$e = 1.6 \times 10^{-19} \text{ C}$$

impractical

Now imagine that we have 2 small bags of charges

bag # 1: Q_1

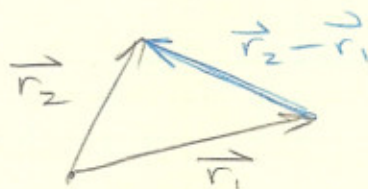
bag # 2: Q_2

Q_1 & Q_2 can be positive or negative

$\vec{F}_{1,2}$: force on Q_2 due to the presence of Q_1

$$\vec{F}_{1,2} = k \frac{Q_1 Q_2}{|\vec{r}_1 - \vec{r}_2|^2}$$

\vec{r}_1 : origin to bag 1
 \vec{r}_2 : origin to bag 2



$|\vec{r}_2 - \vec{r}_1|$: distance between the two bags.

k : proportionality factor

$$k = \frac{1}{4\pi\epsilon_0}$$

ϵ_0 : permittivity of free space.

$$\epsilon_0 = 8.854187 \times 10^{-12} \text{ Fm}^{-1}$$

$$k \sim 9 \times 10^9$$

Recall:

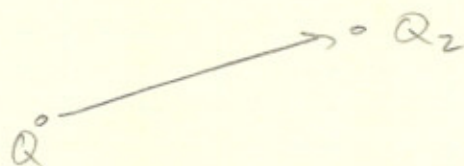
$$\vec{r}_2 = x_2 \hat{x} + y_2 \hat{y} + z_2 \hat{z}$$

$$\vec{r}_1 = x_1 \hat{x} + y_1 \hat{y} + z_1 \hat{z}$$

$$\vec{r}_2 - \vec{r}_1 = (x_2 - x_1) \hat{x} + (y_2 - y_1) \hat{y} + (z_2 - z_1) \hat{z}$$

$$|\vec{r}_2 - \vec{r}_1| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

Now we are interested in the direction of $\vec{F}_{1,2}$.



The force is along $\vec{r}_{12} = \frac{\vec{r}_2 - \vec{r}_1}{|\vec{r}_2 - \vec{r}_1|}$

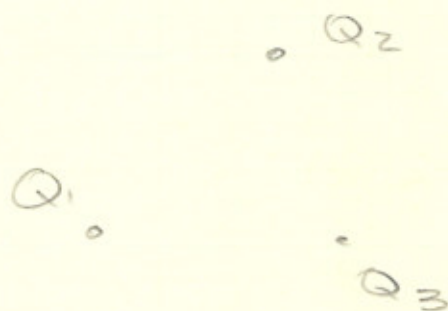
$$\therefore \vec{F}_{1,2} = \frac{Q_1 Q_2}{4\pi\epsilon_0} \frac{\vec{r}_2 - \vec{r}_1}{|\vec{r}_2 - \vec{r}_1|^3}$$

And

$$\vec{F}_{1,2} = -\vec{F}_{2,1}$$

Note: to bags of like charge repel
and bags of unlike charge attract

Super Position Principle



The net force on Q_3 is the sum of the two forces.

$$\vec{F}_3 = \vec{F}_{13} + \vec{F}_{23}$$

$$\vec{E}(\vec{r}_3) = \frac{\vec{F}_3}{Q_3}$$